

B.Tech (Fourth Semester Computer Science & Engineering (C.B.C.S))
End Semester Examination Summer – 2023

Course Name: Theoretical Foundation of Computer Science

Course Code: **BCS2405**
Time: 3 Hours]



ADS/ EFV5738I/3101
[Max.Marks: 60

Instructions to Candidates:

1. All questions carry marks as indicated.
2. All the sub- questions (a, b, c, d, and e) of Que.1 in Section A are compulsory.
3. Solve any two sub-questions in Que. 2 to Que.6 in Section B.
4. Assume suitable data wherever necessary.
5. Use of non-programmable calculator is permitted.

Section – A

Que.1

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|---|---------|
| a) Describe Pigeon Hole Principle. | 2 (CO1) |
| b) Discuss the purpose of pumping lemma? Explain it with example. | 2 (CO2) |
| c) Show that the context free languages are closed under the property of closure and union. | 2 (CO3) |
| d) Write a short note on universal Turing machine. | 2 (CO4) |
| e) Write short note on undecidability. | 2 (CO5) |

Section – B

Que.2

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|---|---------|
| a) Explain Proof by Induction and Contradiction with example. | 5 (CO1) |
| b) Give Mathematical definition of Finite Automata. | 5 (CO1) |
| c) Construct DFA for $L = \{x \in \{a, b\}^* : x _a = \text{odd and } x _b = \text{even}\}$. | 5 (CO1) |

Que.3

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|---|---------|
| a) Construct Moore Machine to determine residue mod 4 for each binary string treated as binary integer. | 5 (CO2) |
| b) Construct DFA for given Regular Expression, $RE = (0+1)(01+10)^*$. | 5 (CO2) |
| c) Find regular grammar that generate the following language $L(aa^*(ab+a)^*)$. | 5 (CO2) |

Que.4

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|--|---------|
| a) Let G be the grammar whose productions are $S \rightarrow aB \mid bA$ $A \rightarrow a \mid aS \mid bAA$ $B \rightarrow b \mid bS \mid Abb$ Find LMD, RMD and Parse Tree for the string “aaabbabbba”. | 5 (CO3) |
| b) Eliminate epsilon production from the given grammar $S \rightarrow aSB \mid aA \mid bB$; $A \rightarrow aA \mid \epsilon$; $B \rightarrow bB \mid \epsilon$ | 5 (CO3) |
| c) Give formal definition of PDA with block diagram. Explain it. | 5 (CO3) |

Que.5

- a) Design T.M. for language to find 2's complement of a binary number. 5 (CO4)
- b) List and explain the variants of a Turing machine. 5 (CO4)
- c) Design a Turing Machine for following language. 5 (CO4)
 $L = \{ a^n b^n c^n \mid n \geq 1 \}$

Que.6

- a) Give Ackermann's function and obtain solution for A (2, 5) and A (3,3). 5 (CO5)
- b) Explain the properties of recursive enumerable language. 5 (CO5)
- c) Describe is PCP and modified PCP. 5 (CO5)

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